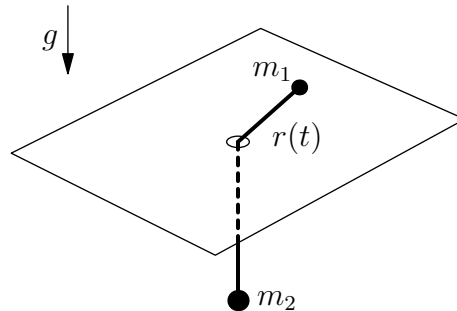


J00M.3—Orbiting Mass on a String

Problem

A mass m_1 slides without friction on a horizontal table. The mass is tied to a string with negligible mass that passes without friction through a small hole. A mass m_2 is tied to the other end of the string. The uniform gravitational acceleration g is normal to the table.



The orbit of m_1 is only slightly perturbed from circular. The masses m_1 and m_2 are chosen so the orbit is closed, with one maximum and one minimum of the distance $r(t)$ of m_1 from the hole, when computed to first order in the departure from a circular orbit. Find m_2 in terms of the other parameters.