M00Q.2—Hyperfine Structure

Problem

The hyperfine energy structure of a hydrogen atom in the 1s level in a constant magnetic field \vec{B} may be represented by the Hamiltonian

$$H = 4\alpha \vec{s}_p \cdot \vec{s}_e + 2\beta \vec{s}_p \cdot \vec{B} + 2\gamma \vec{s}_e \cdot \vec{B}$$

where α , β , and γ are constants and the spin observables are $\vec{s_p}$ and $\vec{s_e}$.

Find the energy eigenvalues.