## J06Q. 2 - Two Indistinguishable Bosons

## Problem

Consider two indistinguishable nonrelativistic bosons of mass $m$, constrained to move one dimensionally around a circle of perimeter $L$ (equivalently, on a line of length $L$ with periodic boundary conditions). The two particles interact via a potential that is a delta-function, $V\left(x_{1}, x_{2}\right)=g \delta\left(x_{1}-x_{2}\right)$. This interaction may be of either sign and of any strength. Give answers for all values of $g$, including $g=0$.
a) The particles have spin zero. Solve for the wave function, energy and degeneracy of the ground state(s). Some of your answers here and below may involve a parameter that you may define as the solution to a transcendental equation.
b) Now the particles have spin one. The interaction is spin-independent. Again, find the wave function(s) (including the spin component), energy, degeneracy and total spin of the ground state(s). Also, find the total spin and the degeneracy of the lowest-energy excited state(s) for each value of $g$.

