## M06M. 1 - Point Mass in a Sphere

## Problem

A point mass $m$ slides without friction inside of a hollow sphere of mass $M$ and radius $R$, that rolls without slipping over a horizontal surface.

a) Find the Lagrangian of this system. Assume that the velocities of the point mass and the sphere are always in the plane of the paper.
b) Consider small amplitude oscillations about the equilibrium position. Express the oscillation frequency in terms of $m, M, R$ and the gravitational constant $g$.

