

3. A plane electromagnetic wave with  $\vec{E} = E_i \exp(ikz - i\omega t)\hat{x}$  is incident from vacuum onto a weakly conductive medium with electrical conductivity  $\sigma$ , dielectric constant  $\epsilon$ , and magnetic permeability  $\mu$ . The medium extends through all space for  $z > 0$ .
- (a) Find the wavenumber  $k(\omega)$  for the plane wave transmitted into the medium.
- (b) Find the electric field amplitude  $E_t$  of the wave transmitted into the medium at a distance  $z = d$  inside the medium, accurate to first order in  $\sigma$ .